

**EIGHTH EDITION**

# Statistics for Business and Economics

**Global Edition**

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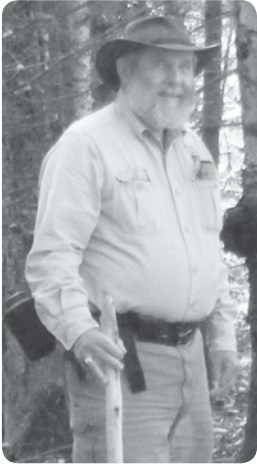
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