

6TH
EDITION

Business Analytics: Data Analysis and Decision Making

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*Bonus Online Material for this text can be found on the text companion website at cengagebrain.com.

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