



INTRODUCTION TO PROBABILITY AND STATISTICS FOR ENGINEERS AND SCIENTISTS

▪ Third Edition ▪

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CONTENTS

| | |
|---|------|
| Preface | xiii |
| Chapter 1 Introduction to Statistics | 1 |
| 1.1 Introduction | 1 |
| 1.2 Data Collection and Descriptive Statistics | 1 |
| 1.3 Inferential Statistics and Probability Models | 2 |
| 1.4 Populations and Samples | 3 |
| 1.5 A Brief History of Statistics | 3 |
| Problems | 7 |
| Chapter 2 Descriptive Statistics | 9 |
| 2.1 Introduction | 9 |
| 2.2 Describing Data Sets | 9 |
| 2.2.1 Frequency Tables and Graphs | 10 |
| 2.2.2 Relative Frequency Tables and Graphs | 10 |
| 2.2.3 Grouped Data, Histograms, Ogives, and Stem and Leaf Plots | 14 |
| 2.3 Summarizing Data Sets | 17 |
| 2.3.1 Sample Mean, Sample Median, and Sample Mode | 17 |
| 2.3.2 Sample Variance and Sample Standard Deviation | 22 |
| 2.3.3 Sample Percentiles and Box Plots | 24 |
| 2.4 Chebyshev's Inequality | 27 |
| 2.5 Normal Data Sets | 31 |
| 2.6 Paired Data Sets and the Sample Correlation Coefficient | 33 |
| Problems | 41 |
| Chapter 3 Elements of Probability | 55 |
| 3.1 Introduction | 55 |
| 3.2 Sample Space and Events | 56 |
| 3.3 Venn Diagrams and the Algebra of Events | 58 |
| 3.4 Axioms of Probability | 59 |
| 3.5 Sample Spaces Having Equally Likely Outcomes | 61 |
| 3.6 Conditional Probability | 67 |
| 3.7 Bayes' Formula | 70 |

| | |
|--|------------|
| 3.8 Independent Events | 76 |
| Problems | 80 |
| Chapter 4 Random Variables and Expectation | 89 |
| 4.1 Random Variables | 89 |
| 4.2 Types of Random Variables | 92 |
| 4.3 Jointly Distributed Random Variables | 95 |
| 4.3.1 Independent Random Variables | 101 |
| *4.3.2 Conditional Distributions | 105 |
| 4.4 Expectation | 107 |
| 4.5 Properties of the Expected Value | 111 |
| 4.5.1 Expected Value of Sums of Random Variables | 115 |
| 4.6 Variance | 118 |
| 4.7 Covariance and Variance of Sums of Random Variables | 121 |
| 4.8 Moment Generating Functions | 126 |
| 4.9 Chebyshev's Inequality and the Weak Law of Large Numbers | 127 |
| Problems | 130 |
| Chapter 5 Special Random Variables | 141 |
| 5.1 The Bernoulli and Binomial Random Variables | 141 |
| 5.1.1 Computing the Binomial Distribution Function | 147 |
| 5.2 The Poisson Random Variable | 148 |
| 5.2.1 Computing the Poisson Distribution Function | 155 |
| 5.3 The Hypergeometric Random Variable | 156 |
| 5.4 The Uniform Random Variable | 160 |
| 5.5 Normal Random Variables | 168 |
| 5.6 Exponential Random Variables | 175 |
| *5.6.1 The Poisson Process | 179 |
| *5.7 The Gamma Distribution | 182 |
| 5.8 Distributions Arising from the Normal | 185 |
| 5.8.1 The Chi-Square Distribution | 185 |
| *5.8.1.1 The Relation Between Chi-Square and Gamma Random Variables | 187 |
| 5.8.2 The t -Distribution | 189 |
| 5.8.3 The F -Distribution | 191 |
| *5.9 The Logistics Distribution | 192 |
| Problems | 194 |
| Chapter 6 Distributions of Sampling Statistics | 201 |
| 6.1 Introduction | 201 |
| 6.2 The Sample Mean | 202 |
| 6.3 The Central Limit Theorem | 204 |

| | | |
|------------------|---|------------|
| 6.3.1 | Approximate Distribution of the Sample Mean | 210 |
| 6.3.2 | How Large a Sample is Needed? | 212 |
| 6.4 | The Sample Variance | 213 |
| 6.5 | Sampling Distributions from a Normal Population | 214 |
| 6.5.1 | Distribution of the Sample Mean | 215 |
| 6.5.2 | Joint Distribution of \bar{X} and S^2 | 215 |
| 6.6 | Sampling from a Finite Population | 217 |
| | Problems | 221 |
| Chapter 7 | Parameter Estimation | 229 |
| 7.1 | Introduction | 229 |
| 7.2 | Maximum Likelihood Estimators | 230 |
| *7.2.1 | Estimating Life Distributions | 238 |
| 7.3 | Interval Estimates | 240 |
| 7.3.1 | Confidence Interval for a Normal Mean When the Variance is Unknown | 246 |
| 7.3.2 | Confidence Intervals for the Variances of a Normal Distribution | 251 |
| 7.4 | Estimating the Difference in Means of Two Normal Populations | 253 |
| 7.5 | Approximate Confidence Interval for the Mean of a Bernoulli Random Variable | 260 |
| *7.6 | Confidence Interval of the Mean of the Exponential Distribution | 265 |
| *7.7 | Evaluating a Point Estimator | 266 |
| *7.8 | The Bayes Estimator | 272 |
| | Problems | 277 |
| Chapter 8 | Hypothesis Testing | 291 |
| 8.1 | Introduction | 291 |
| 8.2 | Significance Levels | 292 |
| 8.3 | Tests Concerning the Mean of a Normal Population | 293 |
| 8.3.1 | Case of Known Variance | 293 |
| 8.3.2 | Case of Unknown Variance: The t -Test | 305 |
| 8.4 | Testing the Equality of Means of Two Normal Populations | 312 |
| 8.4.1 | Case of Known Variances | 312 |
| 8.4.2 | Case of Unknown Variances | 314 |
| 8.4.3 | Case of Unknown and Unequal Variances | 318 |
| 8.4.4 | The Paired t -Test | 319 |
| 8.5 | Hypothesis Tests Concerning the Variance of a Normal Population | 321 |
| 8.5.1 | Testing for the Equality of Variances of Two Normal Populations | 322 |
| 8.6 | Hypothesis Tests in Bernoulli Populations | 323 |
| 8.6.1 | Testing the Equality of Parameters in Two Bernoulli Populations | 327 |

| | |
|--|------------|
| 8.7 Tests Concerning the Mean of a Poisson Distribution | 330 |
| 8.7.1 Testing the Relationship Between Two Poisson Parameters | 331 |
| Problems | 334 |
| Chapter 9 Regression | 351 |
| 9.1 Introduction | 351 |
| 9.2 Least Squares Estimators of the Regression Parameters | 353 |
| 9.3 Distribution of the Estimators | 355 |
| 9.4 Statistical Inferences about the Regression Parameters | 361 |
| 9.4.1 Inferences Concerning β | 362 |
| 9.4.1.1 Regression to the Mean | 366 |
| 9.4.2 Inferences Concerning α | 370 |
| 9.4.3 Inferences Concerning the Mean Response $\alpha + \beta x_0$ | 371 |
| 9.4.4 Prediction Interval of a Future Response | 373 |
| 9.4.5 Summary of Distributional Results | 375 |
| 9.5 The Coefficient of Determination and the Sample Correlation Coefficient | 376 |
| 9.6 Analysis of Residuals: Assessing the Model | 378 |
| 9.7 Transforming to Linearity | 381 |
| 9.8 Weighted Least Squares | 384 |
| 9.9 Polynomial Regression | 391 |
| *9.10 Multiple Linear Regression | 394 |
| 9.10.1 Predicting Future Responses | 405 |
| 9.11 Logistic Regression Models for Binary Output Data | 410 |
| Problems | 413 |
| Chapter 10 Analysis of Variance | 439 |
| 10.1 Introduction | 439 |
| 10.2 An Overview | 440 |
| 10.3 One-Way Analysis of Variance | 442 |
| 10.3.1 Multiple Comparisons of Sample Means | 450 |
| 10.3.2 One-Way Analysis of Variance with Unequal Sample Sizes | 452 |
| 10.4 Two-Factor Analysis of Variance: Introduction and Parameter Estimation | 454 |
| 10.5 Two-Factor Analysis of Variance: Testing Hypotheses | 458 |
| 10.6 Two-Way Analysis of Variance with Interaction | 463 |
| Problems | 471 |
| Chapter 11 Goodness of Fit Tests and Categorical Data Analysis | 483 |
| 11.1 Introduction | 483 |
| 11.2 Goodness of Fit Tests When all Parameters are Specified | 484 |
| 11.2.1 Determining the Critical Region by Simulation | 490 |
| 11.3 Goodness of Fit Tests When Some Parameters are Unspecified | 493 |
| 11.4 Tests of Independence in Contingency Tables | 495 |

| | |
|---|-----|
| 11.5 Tests of Independence in Contingency Tables Having Fixed Marginal Totals | 499 |
| *11.6 The Kolmogorov–Smirnov Goodness of Fit Test for Continuous Data | 504 |
| Problems | 508 |
| Chapter 12 Nonparametric Hypothesis Tests | 515 |
| 12.1 Introduction | 515 |
| 12.2 The Sign Test | 515 |
| 12.3 The Signed Rank Test | 519 |
| 12.4 The Two-Sample Problem | 525 |
| 12.4.1 The Classical Approximation and Simulation | 529 |
| 12.5 The Runs Test for Randomness | 533 |
| Problems | 537 |
| Chapter 13 Quality Control | 545 |
| 13.1 Introduction | 545 |
| 13.2 Control Charts for Average Values: The \bar{X} -Control Chart | 546 |
| 13.2.1 Case of Unknown μ and σ | 549 |
| 13.3 S-Control Charts | 554 |
| 13.4 Control Charts for the Fraction Defective | 557 |
| 13.5 Control Charts for Number of Defects | 559 |
| 13.6 Other Control Charts for Detecting Changes in the Population Mean | 563 |
| 13.6.1 Moving-Average Control Charts | 563 |
| 13.6.2 Exponentially Weighted Moving-Average Control Charts | 565 |
| 13.6.3 Cumulative Sum Control Charts | 571 |
| Problems | 573 |
| Chapter 14* Life Testing | 581 |
| 14.1 Introduction | 581 |
| 14.2 Hazard Rate Functions | 581 |
| 14.3 The Exponential Distribution in Life Testing | 584 |
| 14.3.1 Simultaneous Testing — Stopping at the r th Failure | 584 |
| 14.3.2 Sequential Testing | 590 |
| 14.3.3 Simultaneous Testing — Stopping by a Fixed Time | 594 |
| 14.3.4 The Bayesian Approach | 596 |
| 14.4 A Two-Sample Problem | 598 |
| 14.5 The Weibull Distribution in Life Testing | 600 |
| 14.5.1 Parameter Estimation by Least Squares | 602 |
| Problems | 604 |
| Appendix of Tables | 611 |
| Index | 617 |

* Denotes optional material.