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Growth and International Trade

An Introduction to the Overlapping Generations Approach

Second Edition

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