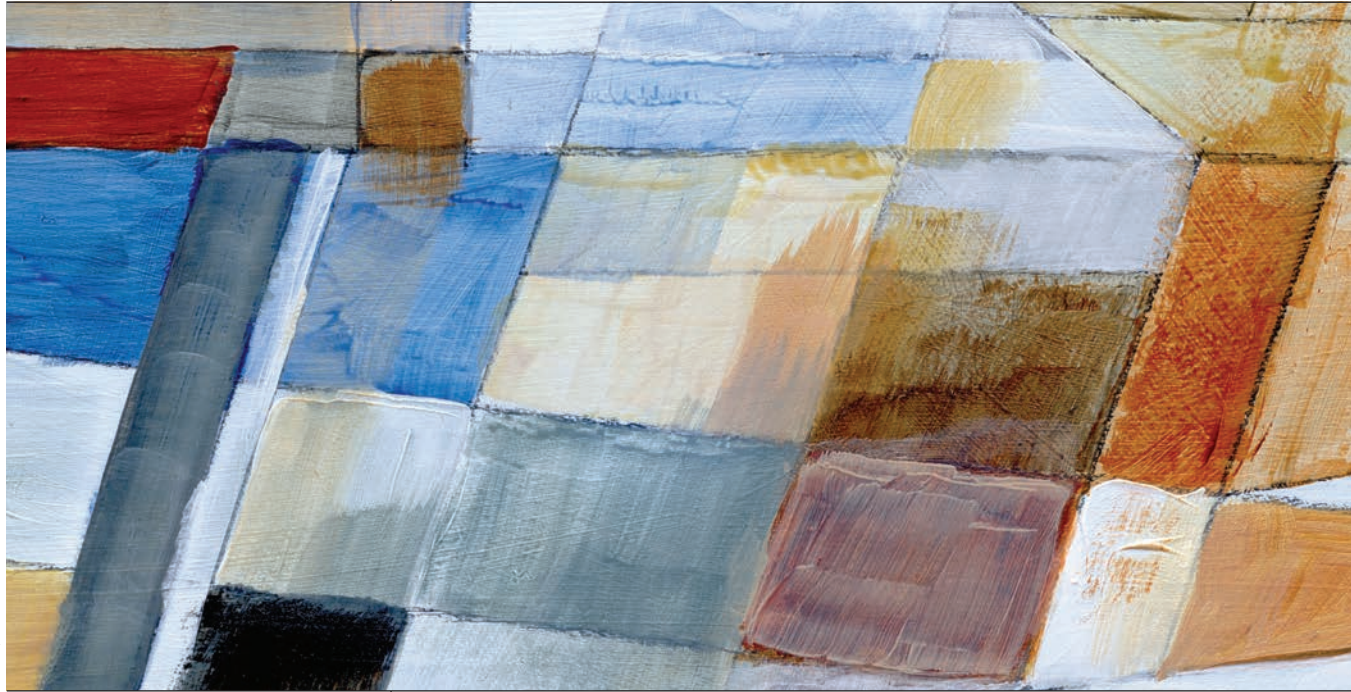


EDITION  
**10**

# Essentials of Statistics FOR THE Behavioral Sciences



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# BRIEF CONTENTS

CHAPTER	<b>1</b>	Introduction to Statistics	1
CHAPTER	<b>2</b>	Frequency Distributions	43
CHAPTER	<b>3</b>	Central Tendency	73
CHAPTER	<b>4</b>	Variability	109
CHAPTER	<b>5</b>	z-Scores: Location of Scores and Standardized Distributions	149
CHAPTER	<b>6</b>	Probability	177
CHAPTER	<b>7</b>	Probability and Samples: The Distribution of Sample Means	213
CHAPTER	<b>8</b>	Introduction to Hypothesis Testing	243
CHAPTER	<b>9</b>	Introduction to the $t$ Statistic	291
CHAPTER	<b>10</b>	The $t$ Test for Two Independent Samples	323
CHAPTER	<b>11</b>	The $t$ Test for Two Related Samples	359
CHAPTER	<b>12</b>	Introduction to Analysis of Variance	391
CHAPTER	<b>13</b>	Two-Factor Analysis of Variance	435
CHAPTER	<b>14</b>	Correlation and Regression	477
CHAPTER	<b>15</b>	The Chi-Square Statistic: Tests for Goodness of Fit and Independence	533

## CHAPTER 1 Introduction to Statistics 1



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### PREVIEW 2

- 1-1 Statistics and Behavioral Sciences 3
- 1-2 Observations, Measurement, and Variables 11
- 1-3 Three Data Structures, Research Methods, and Statistics 19
- 1-4 Statistical Notation 28
- Summary 32
- Focus on Problem Solving 33
- Demonstration 1.1 33
- SPSS® 34
- Problems 38

## CHAPTER 2 Frequency Distributions 43



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### PREVIEW 44

- 2-1 Frequency Distributions and Frequency Distribution Tables 45
- 2-2 Grouped Frequency Distribution Tables 51
- 2-3 Frequency Distribution Graphs 54
- 2-4 Stem and Leaf Displays 62
- Summary 64
- Focus on Problem Solving 65
- Demonstration 2.1 65
- Demonstration 2.2 66
- SPSS® 67
- Problems 70

## CHAPTER 3 Central Tendency 73



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### PREVIEW 74

- 3-1 Overview 75
- 3-2 The Mean 77

3-3 The Median	85
3-4 The Mode	90
3-5 Central Tendency and the Shape of the Distribution	92
3-6 Selecting a Measure of Central Tendency	94
<b>Summary</b>	<b>101</b>
<b>Focus on Problem Solving</b>	<b>101</b>
<b>Demonstration 3.1</b>	<b>102</b>
<b>SPSS®</b>	<b>102</b>
<b>Problems</b>	<b>106</b>

## CHAPTER 4 Variability 109



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<b>PREVIEW</b>	<b>110</b>
4-1 Introduction to Variability	111
4-2 Defining Variance and Standard Deviation	116
4-3 Measuring Variance and Standard Deviation for a Population	121
4-4 Measuring Variance and Standard Deviation for a Sample	124
4-5 Sample Variance as an Unbiased Statistic	130
4-6 More about Variance and Standard Deviation	133
<b>Summary</b>	<b>141</b>
<b>Focus on Problem Solving</b>	<b>142</b>
<b>Demonstration 4.1</b>	<b>142</b>
<b>SPSS®</b>	<b>143</b>
<b>Problems</b>	<b>145</b>

## CHAPTER 5 z-Scores: Location of Scores and Standardized Distributions 149



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<b>PREVIEW</b>	<b>150</b>
5-1 Introduction	151
5-2 z-Scores and Locations in a Distribution	152
5-3 Other Relationships between $z$ , $X$ , the Mean, and the Standard Deviation	157
5-4 Using z-Scores to Standardize a Distribution	160

5-5 Other Standardized Distributions Based on z-Scores	164
5-6 Looking Ahead to Inferential Statistics	167
<b>Summary</b>	<b>170</b>
<b>Focus on Problem Solving</b>	<b>170</b>
<b>Demonstration 5.1</b>	<b>171</b>
<b>Demonstration 5.2</b>	<b>171</b>
<b>SPSS®</b>	<b>172</b>
<b>Problems</b>	<b>174</b>

## CHAPTER 6 Probability 177



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### PREVIEW 178

6-1 Introduction to Probability	179
6-2 Probability and the Normal Distribution	184
6-3 Probabilities and Proportions for Scores from a Normal Distribution	192
6-4 Percentiles and Percentile Ranks	198
6-5 Looking Ahead to Inferential Statistics	203
<b>Summary</b>	<b>205</b>
<b>Focus on Problem Solving</b>	<b>206</b>
<b>Demonstration 6.1</b>	<b>206</b>
<b>SPSS®</b>	<b>207</b>
<b>Problems</b>	<b>210</b>

## CHAPTER 7 Probability and Samples: The Distribution of Sample Means 213



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### PREVIEW 214

7-1 Samples, Populations, and the Distribution of Sample Means	214
7-2 Shape, Central Tendency, and Variability for the Distribution of Sample Means	219
7-3 z-Scores and Probability for Sample Means	226
7-4 More about Standard Error	230
7-5 Looking Ahead to Inferential Statistics	235

Summary 238  
Focus on Problem Solving 239  
Demonstration 7.1 239  
SPSS® 240  
Problems 240

## CHAPTER 8 Introduction to Hypothesis Testing 243



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**PREVIEW 244**  
8-1 The Logic of Hypothesis Testing 244  
8-2 Uncertainty and Errors in Hypothesis Testing 256  
8-3 More about Hypothesis Tests 261  
8-4 Directional (One-Tailed) Hypothesis Tests 266  
8-5 Concerns about Hypothesis Testing: Measuring Effect Size 270  
8-6 Statistical Power 274  
**Summary 283**  
**Focus on Problem Solving 284**  
**Demonstration 8.1 285**  
**Demonstration 8.2 285**  
**Demonstration 8.3 286**  
**SPSS® 287**  
**Problems 287**

## CHAPTER 9 Introduction to the $t$ Statistic 291



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**PREVIEW 292**  
9-1 The  $t$  Statistic: An Alternative to  $z$  292  
9-2 Hypothesis Tests with the  $t$  Statistic 298  
9-3 Measuring Effect Size for the  $t$  Statistic 303  
9-4 Directional Hypotheses and One-Tailed Tests 312  
**Summary 315**  
**Focus on Problem Solving 316**  
**Demonstration 9.1 316**  
**Demonstration 9.2 317**



SPSS® 317  
Problems 319

## CHAPTER 10 The $t$ Test for Two Independent Samples 323



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### PREVIEW 324

- 10-1 Introduction to the Independent-Measures Design 324
- 10-2 The Hypotheses and the Independent-Measures  $t$  Statistic 326
- 10-3 Hypothesis Tests with the Independent-Measures  $t$  Statistic 334
- 10-4 Effect Size and Confidence Intervals for the Independent-Measures  $t$  340
- 10-5 The Role of Sample Variance and Sample Size in the Independent-Measures  $t$  Test 345

### Summary 348

### Focus on Problem Solving 349

### Demonstration 10.1 349

### Demonstration 10.2 351

### SPSS® 351

### Problems 354

## CHAPTER 11 The $t$ Test for Two Related Samples 359



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### PREVIEW 360

- 11-1 Introduction to Repeated-Measures Designs 360
- 11-2 The  $t$  Statistic for a Repeated-Measures Research Design 362
- 11-3 Hypothesis Tests for the Repeated-Measures Design 366
- 11-4 Effect Size, Confidence Intervals, and the Role of Sample Size and Sample Variance for the Repeated-Measures  $t$  369
- 11-5 Comparing Repeated- and Independent-Measures Designs 375

### Summary 380

### Focus on Problem Solving 380

### Demonstration 11.1 381

### Demonstration 11.2 382

### SPSS® 382

### Problems 384

## CHAPTER 12 Introduction to Analysis of Variance 391



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### PREVIEW 392

- 12-1 Introduction: An Overview of Analysis of Variance 392
- 12-2 The Logic of Analysis of Variance 397
- 12-3 ANOVA Notation and Formulas 401
- 12-4 Examples of Hypothesis Testing and Effect Size with ANOVA 409
- 12-5 Post Hoc Tests 416
- 12-6 More about ANOVA 420
- Summary 425
- Focus on Problem Solving 426
- Demonstration 12.1 426
- Demonstration 12.2 428
- SPSS® 428
- Problems 431

## CHAPTER 13 Two-Factor Analysis of Variance 435



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### PREVIEW 436

- 13-1 An Overview of the Two-Factor, Independent-Measures ANOVA 437
- 13-2 An Example of the Two-Factor ANOVA and Effect Size 446
- 13-3 More about the Two-Factor ANOVA 456
- Summary 462
- Focus on Problem Solving 463
- Demonstration 13.1 464
- SPSS® 466
- Problems 471

## CHAPTER 14 Correlation and Regression 477



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### PREVIEW 478

- 14-1 Introduction 479
- 14-2 The Pearson Correlation 482
- 14-3 Using and Interpreting the Pearson Correlation 487
- 14-4 Hypothesis Tests with the Pearson Correlation 494
- 14-5 Alternatives to the Pearson Correlation 498
- 14-6 Introduction to Linear Equations and Regression 507



Summary	520
Focus on Problem Solving	522
Demonstration 14.1	522
SPSS®	524
Problems	528

## CHAPTER 15

## The Chi-Square Statistic: Tests for Goodness of Fit and Independence

533



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### PREVIEW 534

15-1 Introduction to Chi-Square: The Test for Goodness of Fit	534
15-2 An Example of the Chi-Square Test for Goodness of Fit	540
15-3 The Chi-Square Test for Independence	546
15-4 Effect Size and Assumptions for the Chi-Square Tests	553

### Summary 558

### Focus on Problem Solving 559

### Demonstration 15.1 560

### Demonstration 15.2 562

### SPSS® 562

### Problems 565

## APPENDIXES

### A Basic Mathematics Review 569

A-1 Symbols and Notation 571

A-2 Proportions: Fractions, Decimals, and Percentages 573

A-3 Negative Numbers 579

A-4 Basic Algebra: Solving Equations 581

A-5 Exponents and Square Roots 584

### B Statistical Tables 591

### C Solutions for Odd-Numbered Problems in the Text 603

### D General Instructions for Using SPSS® 629

### Statistics Organizer: Finding the Right Statistics for Your Data 635

### Summary of Statistics Formulas 647

### References 651

### Name Index 657

### Subject Index 659