

Elementary Statistics

A S T E P B Y S T E P A P P R O A C H

Tenth Edition



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(www.mhhe.com/bluman)

- Algebra Review
- Writing the Research Report
- Bayes' Theorem
- Alternate Approach to the Standard Normal Distribution
- Bibliography