# An Introduction to Management Science

**Quantitative Approaches to Decision Making** 

Fifteenth Edition



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