

# Modern Statistics for the Social and Behavioral Sciences

*A Practical Introduction*

SECOND EDITION

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# CONTENTS

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<b>CHAPTER 1 ■ INTRODUCTION</b>	<b>1</b>
1.1 SAMPLES VERSUS POPULATIONS	2
1.2 SOFTWARE	2
1.3 R BASICS	3
1.3.1 Entering Data	3
1.3.2 R Functions and Packages	8
1.3.3 Data Sets	10
1.3.4 Arithmetic Operations	11
<b>CHAPTER 2 ■ NUMERICAL AND GRAPHICAL SUMMARIES OF DATA</b>	<b>15</b>
2.1 BASIC SUMMATION NOTATION	16
2.2 MEASURES OF LOCATION	17
2.2.1 The Sample Mean	18
2.2.2 R Function Mean	19
2.2.3 The Sample Median	20
2.2.4 R Function for the Median	22
2.3 A CRITICISM OF THE MEDIAN: IT MIGHT TRIM TOO MANY VALUES	22
2.3.1 R Function for the Trimmed Mean	23
2.3.2 A Winsorized Mean	23
2.3.3 R Function winmean	24
2.3.4 What is a Measure of Location?	25
2.4 MEASURES OF VARIATION OR SCALE	25
2.4.1 Sample Variance and Standard Deviation	25
2.4.2 R Functions var and sd	26
2.4.3 The Interquartile Range	27
2.4.4 R Functions idealf and ideaffQR	28
2.4.5 Winsorized Variance	28
2.4.6 R Function winvar	28
2.4.7 Median Absolute Deviation	28
2.4.8 R Function mad	29
2.4.9 Average Absolute Distance from the Median	29

2.4.10	Other Robust Measures of Variation	29
2.4.11	R Functions bivar, pbvar, tauvar, and tbs	30
<b>2.5</b>	<b>DETECTING OUTLIERS</b>	<b>32</b>
2.5.1	A Method Based on the Mean and Variance	32
2.5.2	A Better Outlier Detection Rule: The MAD-Median Rule	33
2.5.3	R Function out	33
2.5.4	The Boxplot	34
2.5.5	R Function boxplot	35
2.5.6	Modifications of the Boxplot Rule for Detecting Outliers	36
2.5.7	R Function outbox	36
2.5.8	Other Measures of Location	37
2.5.9	R Functions mom and onestep	39
<b>2.6</b>	<b>HISTOGRAMS</b>	<b>39</b>
2.6.1	R Functions hist and splot	42
<b>2.7</b>	<b>KERNEL DENSITY ESTIMATORS</b>	<b>43</b>
2.7.1	R Functions kdplot and akerd	45
<b>2.8</b>	<b>STEM-AND-LEAF DISPLAYS</b>	<b>46</b>
2.8.1	R Function stem	48
<b>2.9</b>	<b>SKEWNESS</b>	<b>49</b>
2.9.1	Transforming Data	49
<b>2.10</b>	<b>CHOOSING A MEASURE OF LOCATION</b>	<b>49</b>
<b>2.11</b>	<b>EXERCISES</b>	<b>51</b>
<b>CHAPTER</b>	<b>3 ■ PROBABILITY AND RELATED CONCEPTS</b>	<b>55</b>
<b>3.1</b>	<b>BASIC PROBABILITY</b>	<b>56</b>
<b>3.2</b>	<b>EXPECTED VALUES</b>	<b>57</b>
<b>3.3</b>	<b>CONDITIONAL PROBABILITY AND INDEPENDENCE</b>	<b>58</b>
<b>3.4</b>	<b>POPULATION VARIANCE</b>	<b>63</b>
<b>3.5</b>	<b>THE BINOMIAL PROBABILITY FUNCTION</b>	<b>65</b>
3.5.1	R Functions dbinom and pbinom	69
<b>3.6</b>	<b>CONTINUOUS VARIABLES AND THE NORMAL CURVE</b>	<b>69</b>
3.6.1	Computing Probabilities Associated with Normal Curves	71
3.6.2	R Function pnorm	71
3.6.3	R Function qnorm	77
<b>3.7</b>	<b>UNDERSTANDING THE EFFECTS OF NONNORMALITY</b>	<b>77</b>
3.7.1	Skewness	80
<b>3.8</b>	<b>PEARSON'S CORRELATION AND THE POPULATION COVARIANCE (OPTIONAL)</b>	<b>82</b>
3.8.1	Computing the Population Covariance and Pearson's Correlation	84

3.9	SOME RULES ABOUT EXPECTED VALUES	85
3.10	CHI-SQUARED DISTRIBUTIONS	86
3.11	EXERCISES	86
<b>CHAPTER</b>	<b>4 ■ SAMPLING DISTRIBUTIONS AND CONFIDENCE INTERVALS</b>	<b>91</b>
<hr/>		
4.1	RANDOM SAMPLING	92
4.2	SAMPLING DISTRIBUTIONS	92
4.2.1	Sampling Distribution of the Sample Mean	93
4.2.2	Computing Probabilities Associated with the Sample Mean	96
4.3	A CONFIDENCE INTERVAL FOR THE POPULATION MEAN	99
4.3.1	Known Variance	100
4.3.2	Confidence Intervals When $\sigma$ Is Not Known	103
4.3.3	R Functions pt and qt	104
4.3.4	Confidence Interval for the Population Mean Using Student's T	105
4.3.5	R Function t.test	105
4.4	JUDGING LOCATION ESTIMATORS BASED ON THEIR SAMPLING DISTRIBUTION	106
4.4.1	Trimming and Accuracy: Another Perspective	109
4.5	AN APPROACH TO NONNORMALITY: THE CENTRAL LIMIT THEOREM	110
4.6	STUDENT'S T AND NONNORMALITY	111
4.7	CONFIDENCE INTERVALS FOR THE TRIMMED MEAN	118
4.7.1	Estimating the Standard Error of a Trimmed Mean	119
4.7.2	R Function trimse	124
4.7.3	A Confidence Interval for the Population Trimmed Mean	124
4.7.4	R Function trimci	126
4.8	TRANSFORMING DATA	128
4.9	CONFIDENCE INTERVAL FOR THE POPULATION MEDIAN	129
4.9.1	R Function sint	130
4.9.2	Estimating the Standard Error of the Sample Median	130
4.9.3	R Function msmedse	131
4.9.4	More Concerns About Tied Values	131
4.10	A REMARK ABOUT MOM AND M-ESTIMATORS	131
4.11	CONFIDENCE INTERVALS FOR THE PROBABILITY OF SUCCESS	132
4.11.1	R Functions binomci, acbinomci and binomLCO	134
4.12	BAYESIAN METHODS	135
4.13	EXERCISES	136
<b>CHAPTER</b>	<b>5 ■ HYPOTHESIS TESTING</b>	<b>141</b>
<hr/>		
5.1	THE BASICS OF HYPOTHESIS TESTING	142

5.1.1	p-Value or Significance Level	147
5.1.2	Criticisms of Two-Sided Hypothesis Testing and p-Values	149
5.1.3	Summary and Generalization	150
<b>5.2</b>	<b>POWER AND TYPE II ERRORS</b>	<b>151</b>
5.2.1	Understanding How $n$ , $\alpha$ , and $\sigma$ Are Related to Power	154
<b>5.3</b>	<b>TESTING HYPOTHESES ABOUT THE MEAN WHEN <math>\sigma</math> IS NOT KNOWN</b>	<b>157</b>
5.3.1	R Function <code>t.test</code>	158
<b>5.4</b>	<b>CONTROLLING POWER AND DETERMINING THE SAMPLE SIZE</b>	<b>159</b>
5.4.1	Choosing $n$ Prior to Collecting Data	159
5.4.2	R Function <code>power.t.test</code>	159
5.4.3	Stein's Method: Judging the Sample Size When Data Are Available	160
5.4.4	R Functions <code>stein1</code> and <code>stein2</code>	162
<b>5.5</b>	<b>PRACTICAL PROBLEMS WITH STUDENT'S T TEST</b>	<b>162</b>
<b>5.6</b>	<b>HYPOTHESIS TESTING BASED ON A TRIMMED MEAN</b>	<b>166</b>
5.6.1	R Function <code>trimci</code>	167
5.6.2	R Functions <code>stein1.tr</code> and <code>stein2.tr</code>	168
<b>5.7</b>	<b>TESTING HYPOTHESES ABOUT THE POPULATION MEDIAN</b>	<b>169</b>
5.7.1	R Function <code>sintv2</code>	169
<b>5.8</b>	<b>MAKING DECISIONS ABOUT WHICH MEASURE OF LOCATION TO USE</b>	<b>169</b>
<b>5.9</b>	<b>BOOTSTRAP METHODS</b>	<b>170</b>
<b>5.10</b>	<b>BOOTSTRAP-T METHOD</b>	<b>170</b>
5.10.1	Symmetric Confidence Intervals	175
5.10.2	Exact Nonparametric Confidence Intervals for Means Are Impossible	176
<b>5.11</b>	<b>THE PERCENTILE BOOTSTRAP METHOD</b>	<b>176</b>
<b>5.12</b>	<b>INFERENCES ABOUT ROBUST MEASURES OF LOCATION</b>	<b>179</b>
5.12.1	Using the Percentile Method	179
5.12.2	R Functions <code>onesampb</code> , <code>momci</code> , and <code>trimpb</code>	180
5.12.3	The Bootstrap-t Method Based on Trimmed Means	181
5.12.4	R Function <code>trimcibt</code>	182
<b>5.13</b>	<b>ESTIMATING POWER WHEN TESTING HYPOTHESES ABOUT A TRIMMED MEAN</b>	<b>183</b>
5.13.1	R Functions <code>powtlest</code> and <code>powtlan</code>	184
<b>5.14</b>	<b>A BOOTSTRAP ESTIMATE OF STANDARD ERRORS</b>	<b>185</b>
5.14.1	R Function <code>bootse</code>	185
<b>5.15</b>	<b>EXERCISES</b>	<b>185</b>
<b>CHAPTER 6</b>	<b>REGRESSION AND CORRELATION</b>	<b>189</b>
<b>6.1</b>	<b>THE LEAST SQUARES PRINCIPLE</b>	<b>190</b>
<b>6.2</b>	<b>CONFIDENCE INTERVALS AND HYPOTHESIS TESTING</b>	<b>192</b>

6.2.1	Classic Inferential Techniques	196
6.2.2	Multiple Regression	198
6.2.3	R Functions <code>ols</code> and <code>lm</code>	199
6.3	STANDARDIZED REGRESSION	201
6.4	PRACTICAL CONCERNS ABOUT LEAST SQUARES REGRESSION AND HOW THEY MIGHT BE ADDRESSED	203
6.4.1	The Effect of Outliers on Least Squares Regression	204
6.4.2	Beware of Bad Leverage Points	205
6.4.3	Beware of Discarding Outliers Among the $Y$ Values	208
6.4.4	Do Not Assume Homoscedasticity or that the Regression Line is Straight	209
6.4.5	Violating Assumptions When Testing Hypotheses	211
6.4.6	Dealing with Heteroscedasticity: The HC4 Method	211
6.4.7	R Functions <code>olshc4</code> and <code>hc4test</code>	212
6.4.8	Interval Estimation of the Mean Response	213
6.4.9	R Function <code>olshc4band</code>	213
6.5	PEARSON'S CORRELATION AND THE COEFFICIENT OF DETERMINATION	214
6.5.1	A Closer Look at Interpreting $r$	216
6.6	TESTING $H_0: \rho = 0$	220
6.6.1	R Function <code>cor.test</code>	220
6.6.2	R Function <code>pwr.r.test</code>	222
6.6.3	Testing $H_0: \rho = 0$ When There is Heteroscedasticity	223
6.6.4	R Function <code>pcorhc4</code>	223
6.6.5	When Is It Safe to Conclude that Two Variables Are Independent?	224
6.7	A REGRESSION METHOD FOR ESTIMATING THE MEDIAN OF $Y$ AND OTHER QUANTILES	224
6.7.1	R Function <code>rqfit</code>	225
6.8	DETECTING HETEROSCEDASTICITY	226
6.8.1	R Function <code>khomreg</code>	227
6.9	INFERENCES ABOUT PEARSON'S CORRELATION: DEALING WITH HETEROSCEDASTICITY	227
6.9.1	R Function <code>pcorb</code>	229
6.10	BOOTSTRAP METHODS FOR LEAST SQUARES REGRESSION	229
6.10.1	R Functions <code>hc4wtest</code> , <code>olswbtest</code> , and <code>lsfitci</code>	231
6.11	DETECTING ASSOCIATIONS EVEN WHEN THERE IS CURVATURE	232
6.11.1	R Functions <code>indt</code> and <code>medind</code>	232
6.12	QUANTILE REGRESSION	233
6.12.1	R Functions <code>qregci</code> and <code>rqtest</code>	234
6.12.2	A Test for Homoscedasticity Using a Quantile Regression Approach	235
6.12.3	R Function <code>qhomt</code>	236

6.13	REGRESSION: WHICH PREDICTORS ARE BEST?	236
6.13.1	The 0.632 Bootstrap Method	238
6.13.2	R function regpre	238
6.13.3	Least Angle Regression	240
6.13.4	R Function larsR	240
6.14	COMPARING CORRELATIONS	241
6.14.1	R Functions TWOpov and TWOpNOV	242
6.15	CONCLUDING REMARKS	243
6.16	EXERCISES	243
<b>CHAPTER</b>	<b>7 ■ COMPARING TWO INDEPENDENT GROUPS</b>	<b>249</b>
<hr/>		
7.1	STUDENT'S T TEST	251
7.1.1	Choosing the Sample Sizes	252
7.1.2	R Function power.t.test	252
7.2	RELATIVE MERITS OF STUDENT'S T	254
7.3	WELCH'S HETEROSCEDASTIC METHOD FOR MEANS	257
7.3.1	R function t.test	259
7.3.2	Tukey's Three-Decision Rule	260
7.3.3	Nonnormality and Welch's Method	261
7.3.4	Three Modern Insights Regarding Methods for Comparing Means	262
7.4	METHODS FOR COMPARING MEDIANS AND TRIMMED MEANS	262
7.4.1	Yuen's Method for Trimmed Means	262
7.4.2	R Functions yuen and fac2list	263
7.4.3	Comparing Medians	264
7.4.4	R Function msmed	265
7.5	PERCENTILE BOOTSTRAP METHODS FOR COMPARING MEASURES OF LOCATION	265
7.5.1	Using Other Measures of Location	267
7.5.2	Comparing Medians	267
7.5.3	R Function medpb2	268
7.5.4	Some Guidelines on When to Use the Percentile Bootstrap Method	268
7.5.5	R Functions trimpb2, med2g, and pb2gen	268
7.6	BOOTSTRAP-T METHODS FOR COMPARING MEASURES OF LOCATION	270
7.6.1	Comparing Means	270
7.6.2	Bootstrap-t Method When Comparing Trimmed Means	271
7.6.3	R Functions yuenbt and yhbt	272
7.6.4	Estimating Power and Judging the Sample Sizes	274
7.6.5	R Functions powest and pow2an	275
7.7	PERMUTATION TESTS	275

7.8	<b>RANK-BASED AND NONPARAMETRIC METHODS</b>	<b>276</b>
7.8.1	Wilcoxon–Mann–Whitney Test	277
7.8.2	R Functions <code>wmw</code> and <code>wilcox.test</code>	279
7.8.3	Handling Tied Values and Heteroscedasticity	279
7.8.4	Cliff’s Method	279
7.8.5	R Functions <code>cid</code> and <code>cidv2</code>	281
7.8.6	The Brunner–Munzel Method	281
7.8.7	R Functions <code>bmp</code> and <code>loc2dif.ci</code>	284
7.8.8	The Kolmogorov–Smirnov Test	284
7.8.9	R Function <code>ks</code>	285
7.8.10	Comparing All Quantiles Simultaneously: An Extension of the Kolmogorov–Smirnov Test	285
7.8.11	R Function <code>sband</code>	286
7.9	<b>GRAPHICAL METHODS FOR COMPARING GROUPS</b>	<b>287</b>
7.9.1	Error Bars	288
7.9.2	R Functions <code>ebarplot</code> and <code>ebarplot.med</code>	290
7.9.3	Plotting the Shift Function	291
7.9.4	Plotting the Distributions	293
7.9.5	R Function <code>sumplot2g</code>	294
7.9.6	Other Approaches	294
7.10	<b>COMPARING MEASURES OF VARIATION</b>	<b>295</b>
7.10.1	R Function <code>comvar2</code>	296
7.10.2	Brown–Forsythe Method	297
7.10.3	Comparing Robust Measures of Variation	298
7.11	<b>MEASURING EFFECT SIZE</b>	<b>299</b>
7.11.1	R Functions <code>yuenv2</code> and <code>akp.effect</code>	304
7.12	<b>COMPARING CORRELATIONS AND REGRESSION SLOPES</b>	<b>305</b>
7.12.1	R Functions <code>twopcor</code> , <code>twolsreg</code> , and <code>tworegwb</code>	306
7.13	<b>COMPARING TWO BINOMIALS</b>	<b>307</b>
7.13.1	Storer–Kim Method	307
7.13.2	Beal’s Method	308
7.13.3	R Functions <code>twobinom</code> , <code>twobici</code> , <code>bi2KMSv2</code> , and <code>power.prop.test</code>	308
7.13.4	Comparing Two Discrete Distributions	309
7.13.5	R Function <code>disc2com</code>	310
7.14	<b>MAKING DECISIONS ABOUT WHICH METHOD TO USE</b>	<b>310</b>
7.15	<b>EXERCISES</b>	<b>311</b>
<b>CHAPTER</b>	<b>8 ■ COMPARING TWO DEPENDENT GROUPS</b>	<b>317</b>
8.1	<b>THE PAIRED T TEST</b>	<b>319</b>



8.1.1	When Does the Paired T Test Perform Well?	320
8.1.2	R Function <code>t.test</code>	321
<b>8.2</b>	<b>COMPARING ROBUST MEASURES OF LOCATION</b>	<b>322</b>
8.2.1	R Functions <code>yuend</code> , <code>ydbt</code> , and <code>dmedpb</code>	323
8.2.2	Comparing Marginal M-Estimators	327
8.2.3	R Function <code>rmest</code>	328
8.2.4	Measuring Effect Size	328
8.2.5	R Function <code>D.akp.effect</code>	328
<b>8.3</b>	<b>HANDLING MISSING VALUES</b>	<b>329</b>
8.3.1	R Functions <code>rm2miss</code> and <code>rmmismcp</code>	330
<b>8.4</b>	<b>A DIFFERENT PERSPECTIVE WHEN USING ROBUST MEASURES OF LOCATION</b>	<b>331</b>
8.4.1	R Functions <code>loc2dif</code> and <code>l2drnci</code>	331
<b>8.5</b>	<b>THE SIGN TEST</b>	<b>332</b>
8.5.1	R Function <code>signt</code>	332
<b>8.6</b>	<b>WILCOXON SIGNED RANK TEST</b>	<b>333</b>
8.6.1	R Function <code>wilcox.test</code>	334
<b>8.7</b>	<b>COMPARING VARIANCES</b>	<b>335</b>
8.7.1	R Function <code>comdvar</code>	335
<b>8.8</b>	<b>COMPARING ROBUST MEASURES OF SCALE</b>	<b>336</b>
8.8.1	R Function <code>rmrvar</code>	336
<b>8.9</b>	<b>COMPARING ALL QUANTILES</b>	<b>336</b>
8.9.1	R Functions <code>lband</code>	337
<b>8.10</b>	<b>PLOTS FOR DEPENDENT GROUPS</b>	<b>337</b>
8.10.1	R Function <code>g2plotdifxy</code>	338
<b>8.11</b>	<b>EXERCISES</b>	<b>338</b>
<b>CHAPTER 9</b>	<b>ONE-WAY ANOVA</b>	<b>341</b>
<b>9.1</b>	<b>ANALYSIS OF VARIANCE FOR INDEPENDENT GROUPS</b>	<b>343</b>
9.1.1	A Conceptual Overview	343
9.1.2	ANOVA via Least Squares Regression and Dummy Coding	348
9.1.3	R Functions <code>anova</code> , <code>anova1</code> , <code>aov</code> , and <code>fac2list</code>	348
9.1.4	Controlling Power and Choosing the Sample Sizes	352
9.1.5	R Functions <code>power.anova.test</code> and <code>anova.power</code>	352
<b>9.2</b>	<b>DEALING WITH UNEQUAL VARIANCES</b>	<b>353</b>
9.2.1	Welch's Test	354
<b>9.3</b>	<b>JUDGING SAMPLE SIZES AND CONTROLLING POWER WHEN DATA ARE AVAILABLE</b>	<b>357</b>
9.3.1	R Functions <code>bdanova1</code> and <code>bdanova2</code>	360
<b>9.4</b>	<b>TRIMMED MEANS</b>	<b>361</b>

9.4.1	R Functions <code>t1way</code> , <code>t1wayv2</code> , <code>t1wayF</code> , and <code>g5plot</code>	362
9.4.2	Comparing Groups Based on Medians	364
9.4.3	R Function <code>med1way</code>	365
<b>9.5</b>	<b>BOOTSTRAP METHODS</b>	<b>365</b>
9.5.1	A Bootstrap-t Method	365
9.5.2	R Functions <code>t1waybt</code> and <code>BFBANOVA</code>	366
9.5.3	Two Percentile Bootstrap Methods	367
9.5.4	R Functions <code>b1way</code> , <code>pbadepth</code> , and <code>Qanova</code>	370
9.5.5	Choosing a Method	370
<b>9.6</b>	<b>RANDOM EFFECTS MODEL</b>	<b>371</b>
9.6.1	A Measure of Effect Size	373
9.6.2	A Heteroscedastic Method	376
9.6.3	A Method Based on Trimmed Means	377
9.6.4	R Function <code>rananova</code>	378
<b>9.7</b>	<b>RANK-BASED METHODS</b>	<b>379</b>
9.7.1	The Kruskal–Wallis Test	379
9.7.2	R Function <code>kruskal.test</code>	380
9.7.3	Method BDM	381
9.7.4	R Functions <code>bdm</code> and <code>bdmP</code>	382
<b>9.8</b>	<b>EXERCISES</b>	<b>383</b>
<b>CHAPTER 10</b>	<b>■ TWO-WAY AND THREE-WAY DESIGNS</b>	<b>387</b>
<hr/>		
<b>10.1</b>	<b>BASICS OF A TWO-WAY ANOVA DESIGN</b>	<b>387</b>
10.1.1	Interactions	391
10.1.2	R Functions <code>interaction.plot</code> and <code>interplot</code>	395
10.1.3	Interactions When There Are More Than Two Levels	396
<b>10.2</b>	<b>TESTING HYPOTHESES ABOUT MAIN EFFECTS AND INTERACTIONS</b>	<b>398</b>
10.2.1	R function <code>anova</code>	401
10.2.2	Inferences About Disordinal Interactions	402
10.2.3	The Two-Way ANOVA Model	403
<b>10.3</b>	<b>HETEROSCEDASTIC METHODS FOR TRIMMED MEANS, INCLUDING MEANS</b>	<b>404</b>
10.3.1	R Function <code>t2way</code>	405
<b>10.4</b>	<b>BOOTSTRAP METHODS</b>	<b>408</b>
10.4.1	R Functions <code>pbad2way</code> and <code>t2waybt</code>	410
<b>10.5</b>	<b>TESTING HYPOTHESES BASED ON MEDIANS</b>	<b>412</b>
10.5.1	R Function <code>m2way</code>	413
<b>10.6</b>	<b>A RANK-BASED METHOD FOR A TWO-WAY DESIGN</b>	<b>413</b>
10.6.1	R Function <code>bdm2way</code>	414

10.6.2	The Patel–Hoel Approach to Interactions	414
10.7	<b>THREE-WAY ANOVA</b>	<b>415</b>
10.7.1	R Functions <code>anova</code> and <code>t3way</code>	417
10.8	<b>EXERCISES</b>	<b>418</b>
<b>CHAPTER 11</b>	<b>■ COMPARING MORE THAN TWO DEPENDENT GROUPS</b>	<b>421</b>
<hr/>		
11.1	<b>COMPARING MEANS IN A ONE-WAY DESIGN</b>	<b>422</b>
11.1.1	R Function <code>aov</code>	424
11.2	<b>COMPARING TRIMMED MEANS WHEN DEALING WITH A ONE-WAY DESIGN</b>	<b>425</b>
11.2.1	R Functions <code>rmanova</code> and <code>rmdat2mat</code>	426
11.2.2	A Bootstrap-t Method for Trimmed Means	428
11.2.3	R Function <code>rmanovab</code>	429
11.3	<b>PERCENTILE BOOTSTRAP METHODS FOR A ONE-WAY DESIGN</b>	<b>429</b>
11.3.1	Method Based on Marginal Measures of Location	430
11.3.2	R Function <code>bd1way</code>	430
11.3.3	Inferences Based on Difference Scores	431
11.3.4	R Function <code>rmdzero</code>	432
11.4	<b>RANK-BASED METHODS FOR A ONE-WAY DESIGN</b>	<b>432</b>
11.4.1	Friedman’s Test	432
11.4.2	R Function <code>friedman.test</code>	434
11.4.3	Method BPRM	434
11.4.4	R Function <code>bprm</code>	435
11.5	<b>COMMENTS ON WHICH METHOD TO USE</b>	<b>436</b>
11.6	<b>BETWEEN-BY-WITHIN DESIGNS</b>	<b>436</b>
11.6.1	Method for Trimmed Means	437
11.6.2	R Function <code>bwtrim</code> and <code>bw2list</code>	439
11.6.3	A Bootstrap-t Method	441
11.6.4	R Function <code>tsplitbt</code>	441
11.6.5	Inferences Based on M-estimators and Other Robust Measures of Location	442
11.6.6	R Functions <code>sppba</code> , <code>sppbb</code> , and <code>sppbi</code>	443
11.6.7	A Rank-Based Test	444
11.6.8	R Function <code>bwrank</code>	448
11.7	<b>WITHIN-BY-WITHIN DESIGN</b>	<b>449</b>
11.7.1	R Function <code>wwtrim</code>	449
11.8	<b>THREE-WAY DESIGNS</b>	<b>449</b>
11.8.1	R Functions <code>bbwtrim</code> , <code>bwtrim</code> , and <code>wwwtrim</code>	449
11.8.2	Data Management: R Functions <code>bw2list</code> and <code>bbw2list</code>	450
11.9	<b>EXERCISES</b>	<b>451</b>

<b>CHAPTER 12 ■ MULTIPLE COMPARISONS</b>	<b>453</b>
<b>12.1 ONE-WAY ANOVA AND RELATED SITUATIONS, INDEPENDENT GROUPS</b>	<b>455</b>
12.1.1 Fisher's Least Significant Difference Method	455
12.1.2 The Tukey–Kramer Method	457
12.1.3 R Function TukeyHSD	458
12.1.4 Tukey–Kramer and the ANOVA F Test	459
12.1.5 Step-Down Methods	459
12.1.6 Dunnett's T3	462
12.1.7 Games–Howell Method	464
12.1.8 Comparing Trimmed Means	464
12.1.9 R Functions lincon, stepmcp and twoKlin	464
12.1.10 Alternative Methods for Controlling FWE	465
12.1.11 Percentile Bootstrap Methods for Comparing Trimmed Means, Medians, and M-estimators	468
12.1.12 R Functions medpb, linconpb, pbmcp, and p.adjust	469
12.1.13 A Bootstrap-t Method	470
12.1.14 R Function linconbt	470
12.1.15 Rank-Based Methods	471
12.1.16 R Functions cidmul, cidmulv2, and bmpmul	471
12.1.17 Comparing the Individual Probabilities of Two Discrete Distributions	471
12.1.18 R Functions binband, splotg2, cumrelf, and cumrelfT	472
12.1.19 Comparing the Quantiles of Two Independent Groups	473
12.1.20 R Functions qcomhd and qcomhdMC	474
12.1.21 Multiple Comparisons for Binomial and Categorical Data	475
12.1.22 R Functions skmcp and discmcp	475
<b>12.2 TWO-WAY, BETWEEN-BY-BETWEEN DESIGN</b>	<b>475</b>
12.2.1 Scheffé's Homoscedastic Method	477
12.2.2 Heteroscedastic Methods	479
12.2.3 Extension of Welch–Šidák and Kaiser–Bowden Methods to Trimmed Means	481
12.2.4 R Function kbcon	482
12.2.5 R Functions con2way and conCON	482
12.2.6 Linear Contrasts Based on Medians	485
12.2.7 R Functions msmed and mcp2med	485
12.2.8 Bootstrap Methods	486
12.2.9 R Functions mcp2a, bbmcp2pb, bbmcp	487
12.2.10 The Patel–Hoel Rank-Based Interaction Method	487
12.2.11 R Function rimul	487
<b>12.3 JUDGING SAMPLE SIZES</b>	<b>487</b>

12.3.1	Tamhane's Procedure	488
12.3.2	R Function tamhane	489
12.3.3	Hochberg's Procedure	489
12.3.4	R Function hochberg	491
<b>12.4</b>	<b>METHODS FOR DEPENDENT GROUPS</b>	<b>491</b>
12.4.1	Linear Contrasts Based on Trimmed Means	492
12.4.2	R Function rmmcp	493
12.4.3	Comparing M-estimators	493
12.4.4	R Functions rmmcppb, dmedpb, dtrimpb, and boxdif	494
12.4.5	Bootstrap-t Method	494
12.4.6	R Function bptd	495
12.4.7	Comparing the Quantiles of the Marginal Distributions	495
12.4.8	R Function Dqcomhd	495
<b>12.5</b>	<b>BETWEEN-BY-WITHIN DESIGNS</b>	<b>495</b>
12.5.1	R Functions bwmcp, bwamcp, bwbmcp, bwimcp, spmcpa, spmcpb, spmcp, and bwmcppb	497
<b>12.6</b>	<b>WITHIN-BY-WITHIN DESIGNS</b>	<b>499</b>
12.6.1	Three-Way Designs	500
12.6.2	R Functions con3way, mcp3atm, and rm3mcp	500
12.6.3	Bootstrap Methods for Three-Way Designs	502
12.6.4	R Functions bbwmc, bwwmcp, bwwmcppb, bbbmcppb, bbwmcppb, bwwmcppb, and wwwmcppb	502
<b>12.7</b>	<b>EXERCISES</b>	<b>503</b>
<b>CHAPTER 13</b>	<b>■ SOME MULTIVARIATE METHODS</b>	<b>507</b>
<b>13.1</b>	<b>LOCATION, SCATTER, AND DETECTING OUTLIERS</b>	<b>508</b>
13.1.1	Detecting Outliers Via Robust Measures of Location and Scatter	511
13.1.2	R Functions cov.mve and cov.mcd	512
13.1.3	More Measures of Location and Covariance	513
13.1.4	R Functions rmba, tbs, and ogk	514
13.1.5	R Function out	514
13.1.6	A Projection-Type Outlier Detection Method	514
13.1.7	R Functions outpro, outproMC, outproad, outproadMC, and out3d	516
13.1.8	Skipped Estimators of Location	517
13.1.9	R Function smean	517
<b>13.2</b>	<b>ONE-SAMPLE HYPOTHESIS TESTING</b>	<b>518</b>
13.2.1	Comparing Dependent Groups	521
13.2.2	R Functions smeancrv2, hotell, and rmdzeroOP	522
<b>13.3</b>	<b>TWO-SAMPLE CASE</b>	<b>523</b>
13.3.1	R Functions smean2, mat2grp, matsplit, and mat2list	524

13.3.2	R functions matsplit, mat2grp, and mat2list	524
<b>13.4</b>	<b>MANOVA</b>	<b>525</b>
13.4.1	R Function manova	526
13.4.2	Robust MANOVA Based on Trimmed Means	527
13.4.3	R Functions MULtr.anova and MULAOPv	528
<b>13.5</b>	<b>A MULTIVARIATE EXTENSION OF THE WILCOXON–MANN–WHITNEY TEST</b>	<b>529</b>
13.5.1	Explanatory Measure of Effect Size: A Projection-Type Generalization	530
13.5.2	R Function mulwmwv2	531
<b>13.6</b>	<b>RANK-BASED MULTIVARIATE METHODS</b>	<b>531</b>
13.6.1	The Munzel–Brunner Method	532
13.6.2	R Function mulrank	533
13.6.3	The Choi–Marden Multivariate Rank Test	534
13.6.4	R Function cmanova	536
<b>13.7</b>	<b>MULTIVARIATE REGRESSION</b>	<b>536</b>
13.7.1	Multivariate Regression Using R	537
13.7.2	Robust Multivariate Regression	538
13.7.3	R Function mlrreg and mopreg	539
<b>13.8</b>	<b>PRINCIPAL COMPONENTS</b>	<b>539</b>
13.8.1	R Functions precomp and regpca	541
13.8.2	Robust Principal Components	544
13.8.3	R Functions outpca, robpca, robpcaS, Ppca, and Ppca.summary	544
<b>13.9</b>	<b>EXERCISES</b>	<b>547</b>
<b>CHAPTER 14</b>	<b>■ ROBUST REGRESSION AND MEASURES OF ASSOCIATION</b>	<b>549</b>
<b>14.1</b>	<b>ROBUST REGRESSION ESTIMATORS</b>	<b>550</b>
14.1.1	The Theil–Sen Estimator	551
14.1.2	R Functions tsreg, tshdreg, and regplot	552
14.1.3	Least Median of Squares	553
14.1.4	Least Trimmed Squares and Least Trimmed Absolute Value Estimators	553
14.1.5	R Functions lmsreg, ltsreg, and ltareg	554
14.1.6	M-estimators	554
14.1.7	R Function chreg	554
14.1.8	Deepest Regression Line	555
14.1.9	R Function mdepreg	555
14.1.10	Skipped Estimators	555
14.1.11	R Functions opreg and opregMC	555
14.1.12	S-estimators and an E-type Estimator	555
14.1.13	R Function tstsreg	556

14.2	COMMENTS ON CHOOSING A REGRESSION ESTIMATOR	556
14.3	INFERENCES BASED ON ROBUST REGRESSION ESTIMATORS	557
14.3.1	Testing Hypotheses About the Slopes	558
14.3.2	Inferences About the Typical Value of $Y$ Given $X$	558
14.3.3	R Functions <code>regtest</code> , <code>regtestMC</code> , <code>regci</code> , <code>regciMC</code> , <code>regYci</code> , and <code>regYband</code>	559
14.3.4	Comparing Measures of Location via Dummy Coding	563
14.4	DEALING WITH CURVATURE: SMOOTHERS	563
14.4.1	Cleveland's Smoother	564
14.4.2	R Functions <code>lowess</code> , <code>lplot</code> , <code>lplot.pred</code> , and <code>lplotCI</code>	565
14.4.3	Smoother Based on Robust Measures of Location	566
14.4.4	R Functions <code>rplot</code> , <code>rplotCIS</code> , <code>rplotCI</code> , <code>rplotCIv2</code> , <code>rplotCIM</code> , <code>rplot.pred</code> , <code>qhds</code> , and <code>qhds.pred</code>	568
14.4.5	Prediction When $X$ Is Discrete: The R Function <code>rundis</code>	570
14.4.6	Seeing Curvature with More Than Two Predictors	571
14.4.7	R Function <code>prplot</code>	571
14.4.8	Some Alternative Methods	571
14.4.9	Detecting Heteroscedasticity Using a Smoother	573
14.4.10	R Function <code>rhom</code>	573
14.5	SOME ROBUST CORRELATIONS AND TESTS OF INDEPENDENCE	573
14.5.1	Kendall's tau	573
14.5.2	Spearman's rho	574
14.5.3	Winsorized Correlation	575
14.5.4	R Function <code>wincor</code>	575
14.5.5	OP or Skipped Correlation	575
14.5.6	R Function <code>scor</code>	576
14.5.7	Inferences about Robust Correlations: Dealing with Heteroscedasticity	577
14.5.8	R Functions <code>corb</code> and <code>scorci</code>	577
14.6	MEASURING THE STRENGTH OF AN ASSOCIATION BASED ON A ROBUST FIT	577
14.7	COMPARING THE SLOPES OF TWO INDEPENDENT GROUPS	578
14.7.1	R Function <code>reg2ci</code>	579
14.8	TESTS FOR LINEARITY	579
14.8.1	R Functions <code>lintest</code> , <code>lintestMC</code> , and <code>linchk</code>	581
14.9	IDENTIFYING THE BEST PREDICTORS	582
14.9.1	Inferences Based on Independent Variables Taken in Isolation	582
14.9.2	R Functions <code>regpord</code> , <code>ts2str</code> , and <code>sm2strv7</code>	584
14.9.3	Inferences When Independent Variables Are Taken Together	585
14.9.4	R Function <code>regIVcom</code>	587
14.10	INTERACTIONS AND MODERATOR ANALYSES	588

14.10.1	R Functions <code>olshc4.inter</code> , <code>ols.plot.inter</code> , <code>regci.inter</code> , <code>reg.plot.inter</code> and <code>adtest</code>	590
14.10.2	Graphical Methods for Assessing Interactions	591
14.10.3	R Functions <code>kercon</code> , <code>runsm2g</code> , <code>regi</code>	592
<b>14.11</b>	<b>ANCOVA</b>	<b>593</b>
14.11.1	Classic ANCOVA	594
14.11.2	Robust ANCOVA Methods Based on a Parametric Regression Model	596
14.11.3	R Functions <code>ancJN</code> , <code>ancJNmp</code> , <code>anclin</code> , <code>reg2plot</code> , and <code>reg2g.p2plot</code>	597
14.11.4	ANCOVA Based on the Running-interval Smoother	599
14.11.5	R Functions <code>ancsm</code> , <code>Qancsm</code> , <code>ancova</code> , <code>ancovaWMW</code> , <code>anepb</code> , <code>ancovaUB</code> , <code>ancboot</code> , <code>ancdet</code> , <code>runmean2g</code> , <code>qhds2g</code> , and <code>l2plot</code>	600
14.11.6	R Functions <code>Dancts</code> , <code>Dancols</code> , <code>Dancova</code> , <code>Dancovapb</code> , <code>DancovaUB</code> , and <code>Dancdet</code>	604
<b>14.12</b>	<b>EXERCISES</b>	<b>605</b>
<b>CHAPTER 15</b>	<b>■ BASIC METHODS FOR ANALYZING CATEGORICAL DATA</b>	<b>609</b>
<b>15.1</b>	<b>GOODNESS OF FIT</b>	<b>610</b>
15.1.1	R Functions <code>chisq.test</code> and <code>pwr.chisq.test</code>	611
<b>15.2</b>	<b>A TEST OF INDEPENDENCE</b>	<b>612</b>
15.2.1	R Function <code>chi.test.ind</code>	614
<b>15.3</b>	<b>DETECTING DIFFERENCES IN THE MARGINAL PROBABILITIES</b>	<b>615</b>
15.3.1	R Functions <code>contab</code> and <code>mcnemar.test</code>	617
<b>15.4</b>	<b>MEASURES OF ASSOCIATION</b>	<b>618</b>
15.4.1	The Proportion of Agreement	620
15.4.2	Kappa	621
15.4.3	Weighted Kappa	622
15.4.4	R Function <code>Ckappa</code>	622
<b>15.5</b>	<b>LOGISTIC REGRESSION</b>	<b>623</b>
15.5.1	R Functions <code>glm</code> and <code>logreg</code>	623
15.5.2	A Confidence Interval for the Odds Ratio	625
15.5.3	R Function <code>ODDSR.CI</code>	626
15.5.4	Smoothers for Logistic Regression	626
15.5.5	R Functions <code>logrsm</code> , <code>rplot.bin</code> , and <code>logSM</code>	627
<b>15.6</b>	<b>EXERCISES</b>	<b>627</b>
<b>APPENDIX A</b>	<b>■ ANSWERS TO SELECTED EXERCISES</b>	<b>631</b>
<b>APPENDIX B</b>	<b>■ TABLES</b>	<b>635</b>



APPENDIX C ■ BASIC MATRIX ALGEBRA	663
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Index	697
-------	-----